

## WROCLAW UNIVERSITY OF TECHNOLOGY – PHD STUDIES

|  |                                     |
|--|-------------------------------------|
| <b>FACULTY OF .....</b>  |                                     |
| <b>SUBJECT CARD</b>  |                                     |
| Course name in Polish  | <b>Podstawy teorii Galois</b>       |
| Course name in English   | <b>Foundations of Galois Theory</b> |
| Course language  |                                     |
| University-wide general course type: 1)<br>1) basic course (mathematics, physics, chemistry, other)<br>2) humanity course<br>3) managerial skills<br>4) English language<br>5) other modern language<br>Departmental course developing professional skills:<br>1) specialized course<br>2) interdisciplinary course<br>3) seminar (interdisciplinary, specialized, departmental) |                                     |
| Type of course (obligatory, optional)  |                                     |
| <b>Educational effects according to ZW 26/2017: P8S_WG, P8U_U, P8S_UW , P8S_UU, P8S_KK</b><br>.....  |                                     |
| Subject code <b>MAP9030</b>  |                                     |

\*delete as applicable

|   | Lecture | Laboratory                   | Seminar           |
|---|---------|------------------------------|-------------------|
| Number of hours of organized classes in University (ZZU)                        | 30      |                              |                   |
| Number of hours of total student workload (CNPS)                                | 90      |                              |                   |
| Form of crediting   | Exam ** | Exam / crediting with grade* | Oral presentation |
| Number of ECTS points   | 3       |                              |                   |
| including number of ECTS points for practical (P) classes                       |         |                              |                   |
| including number of ECTS points for direct teacher-student contact (BK) classes |         |                              |                   |

\*delete as applicable \*\*In case of didactic courses also inspections and evaluation classes

|  |  |
|--|--|
| <b>PREREQUISITES RELATING TO KNOWLEDGE, SKILLS AND OTHER COMPETENCES</b> |  |
| 1.   | Knowledge of higher algebra - basic course |

|                           |  |
|---------------------------|--|
| <b>SUBJECT OBJECTIVES</b> |  |
| C1                        | Getting acquainted with the main ideas of the Galois theory, in particular the understanding of the relationship between group structure of automorphisms of field and the field extension by radicals |

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|    |   |
|----|---|
| C2 | The possibility of applying Galois theory to specific algebraic equations |
|    |   |
|    |   |

**SUBJECT EDUCATIONAL EFFECTS**

**Relating to knowledge:**

PEK\_W01 – Student has knowledge of group theory

PEK\_W02 – Student has knowledge of field theory

PEK\_W03 – Student has knowledge of Galois theory

**Relating to skills:**

PEK\_U01 – Student can to apply Galois theory to decide which algebraic equation can be solved by radicals

PEK\_U02 – Student can apply methods of mathematical analysis to determine group automorphism of given concrete algebraic equation

...

**Relating to social competences:**

PEK\_K01 – Student understands the importance scientific research and didactics

PEK\_K02 – Student can discuss the importance of solving equations and their methods at the popular science level

...

**PROGRAM CONTENTS**

| <b>Form of classes – lecture</b> |   | Number of hours |
|----------------------------------|---|-----------------|
| Lec 1                            | Group and subgroup notion, group rank, space of cosets, Lagrange theorem  | 2               |
| Lec 2                            | Homomorphism of groups, group of all automorphisms  | 2               |
| Lec 3                            | Normal group, quotient group, theorem on homomorphisms of groups  | 2               |
| Lec 4                            | Symmetric group, decomposition of the group onto cycles, Cayley theorem   | 2               |
| Lec 5                            | Field and subfield notion, algebraically closed field, algebraic closedness of the field of all complex numbers | 2               |
| Lec 6                            | Field extension, theorem on existence of algebraically closed field extension                                   | 2               |
| Lec 7                            | Algebraic elements, transcendental real numbers and two proofs of their existence                               | 2               |
| Lec 8                            | Irreducible polynomials, the Eisenstein theorem, rank of the algebraic element                                  | 2               |
| Lec 9                            | Field extension by the algebraic element, Artin-Schreier theorem on primitive element                           | 2               |

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|             |   |           |
|-------------|---|-----------|
| Lec 10      | Basis and rank of the algebraic extension, minimal polynomial of algebraic element                                      | 2         |
| Lec 11      | Group of automorphisms of field, Galois extension and their group   | 2         |
| Lec 12      | Normal extension. Galois theorems   | 2         |
| Lec 13      | Roots of polynomials of the second, third and fourth degree   | 2         |
| Lec 14      | Field extension by radicals and their relationship with the solvable groups   | 2         |
| Lec 15      | Solvability of $S_4$ group and unsolvability of $S_5$ group, algebraic equation which are not have solution by radicals | 2         |
| Total hours |   | <b>30</b> |

| Form of classes – laboratory |  | Number of hours |
|------------------------------|--|-----------------|
| Lab 1                        |  |                 |
| Lab 2                        |  |                 |
| Lab 3                        |  |                 |
| Lab 4                        |  |                 |
| ...                          |  |                 |
| Total hours                  |  |                 |

| Form of classes – seminar |  | Number of hours |
|---------------------------|--|-----------------|
| Sem 1                     |  |                 |
| Sem 2                     |  |                 |
| Sem 3                     |  |                 |
| Sem 4                     |  |                 |
| ...                       |  |                 |
| Total hours               |  |                 |

| TEACHING TOOLS USED |            |
|---------------------|------------|
| N1                  | Blackboard |
| N2                  | Chalk      |
| ...                 |            |

| EVALUATION OF ACHIEVED SUBJECT EDUCATIONAL EFFECTS            |  |  |
|---|--|--|
| <b>Evaluation:</b><br>F – forming (partial)<br>C – concluding | Educational effect number                                | Way of evaluating achievement of educational effects |
| F1  | PEK_W01,PEK_W02<br>PEK_U01<br>PEK_U02,PEK_K01<br>PEK_K02 | exam   |

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**PRIMARY AND SECONDARY LITERATURE****PRIMARY LITERATURE:**

- [1] W. Narkiewicz, Teoria Galois dla nauczycieli, wyd. UW r 1993
- [2] S. Lange, Algebra, PWN Warszawa, 1984
- [3] A. Białynicki-Birula, Algebra, BM t. 40, PWN 1971, 2014
- [4] A. Białynicki-Birula, Algebra, BM t. 40, PWN 1971, 2014

**SECONDARY LITERATURE:**

- [1] M. Bryński, J. Jurkiewicz, Zbiór zadań z algebry, PWN 1978

**SUBJECT SUPERVISOR**

(NAME AND SURNAME, E-MAIL ADDRESS)

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